

**UNIVERSITY EXAMINATIONS**

**FIRST SEMESTER 2025/2026 ACADEMIC YEAR**

**FOURTH YEAR EXAMINATION FOR THE DEGREE OF  
BACHELOR OF SCIENCE (STATISTICS) AND BACHELOR  
OF SCIENCE (ECOMICS & STATISTICS)**

**STAT 411: APPLIED TIME SERIES ANALYSIS**

***STREAM: R***

***TIME: 2 HRS***

***DAY: MONDAY [8.30 – 10.30 A.M]***

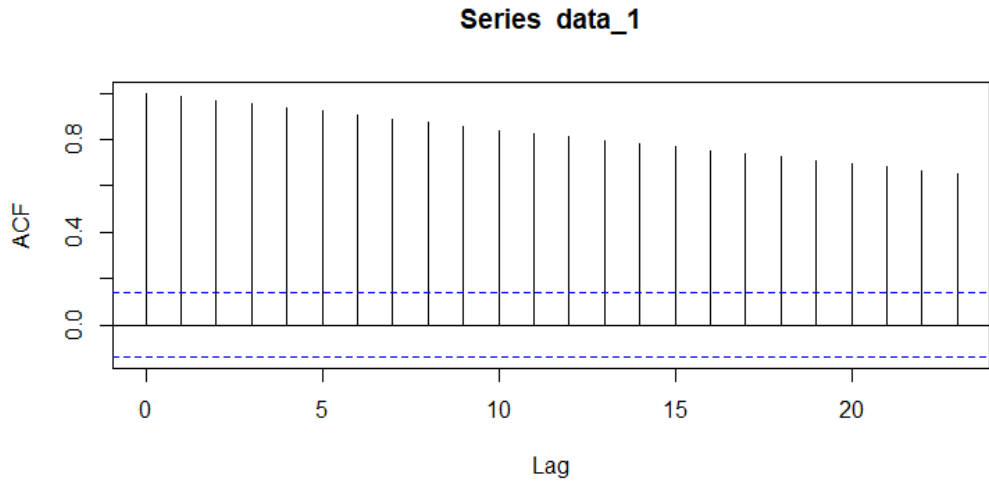
***DATE: 02/02/2026***

**THIS QUESTION PAPER CONSISTS OF FIVE (5) PAGES**

**PLEASE DO NOT OPEN UNTIL THE INVIGILATOR SAYS SO.**

**Instructions: Answer Question ONE (compulsory) and any Other TWO questions**  
**QUESTION ONE (30 MARKS)**

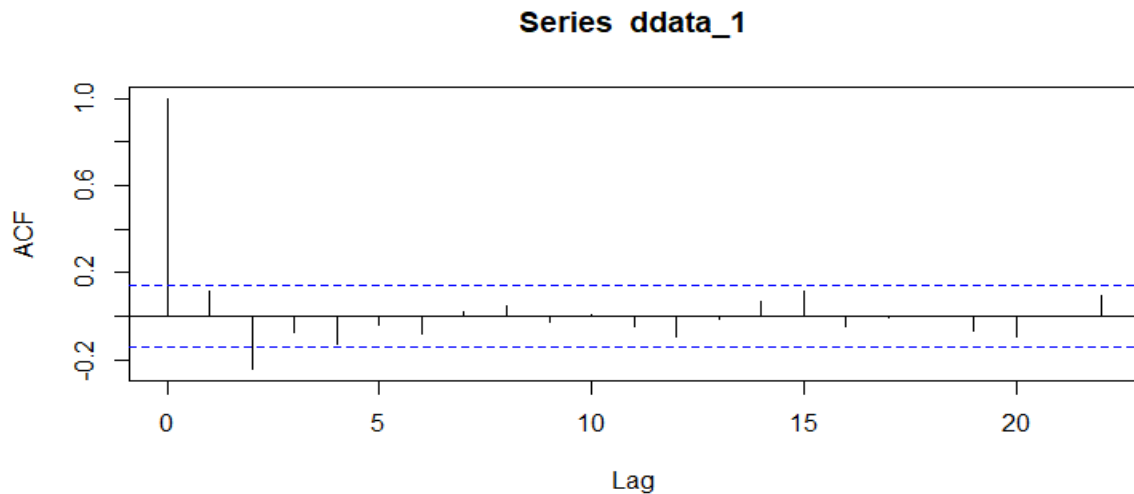
a) Consider the following Autocorrelation function of time series depicted in figure 1



**Figure1**

- i) Is the series stationary or not? Why? **(2 Marks)**
- ii) What kind of transformation is required to make it stationary? **(2 Marks)**

b) Consider the following ACF depicted in the Figure 2 below.

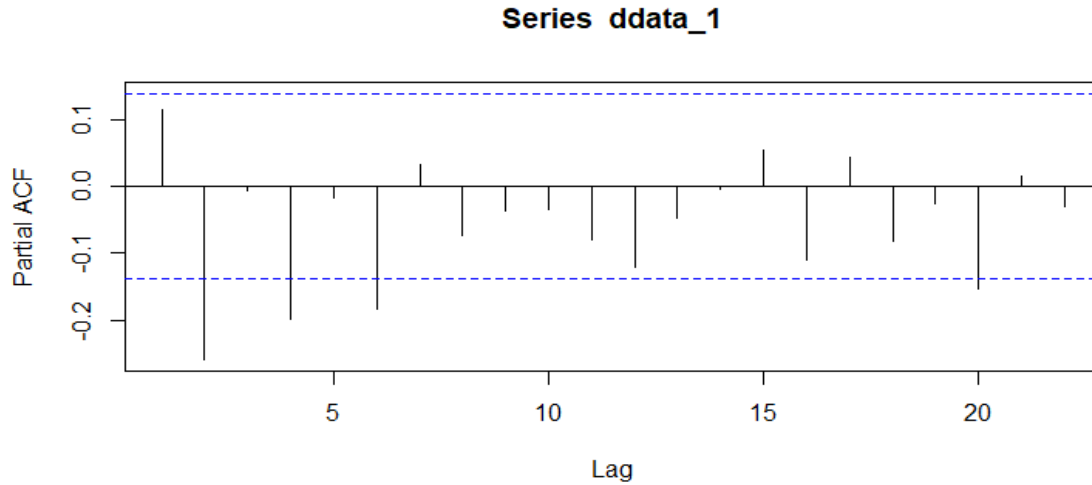


**Figure2**

- i) State the lags of ACF which are significant from the figure 2. **(2 Marks)**

- ii) Which are the possible models for the acf depicted above? (2 Marks)

C) Consider the PACF given in figure 3.



**Figure 3**

- i) Which PACF(s) are significant (2 Marks)  
 ii) Which models are represented by the ACF given Figure 3 (2 Marks)

d)The data below shows quarterly sales ('000) of Sea Company from 2015 to 2017.

Year	Quarte1	Quarter 2	Quarter3	Quarter 4
2015	230	430	100	150
2016	250	480	110	175
2017	290	520	119	208

- i) Compute the trend of the series. Comment on its shape. (3 Marks)  
 ii) Compute the seasonal variations (4 Marks)  
 iii) Forecast sales values for 2018 (4 Marks)
- e) State and verify four properties of the autocovariance function. (7 Marks)

**QUESTION TWO (20 MARKS)**

- a) With the aid of an example, define explain what is meant by time series (4 Marks)
- b) State and explain how forecasting can be applied in three specific business functional areas (6 Marks)

c)\_Given AR(1) process  $X_t = \phi X_{t-1} + e_t$

Find

- i) An optimal one-step-ahead forecast (3 Marks)
- ii) the one step ahead forecast error (2 Marks)
- iii) An optimal two-steps-ahead forecast (3 Marks)
- iv) The two steps ahead forecast error (2 Marks)

**QUESTION THREE (20 MARKS)**

a) Consider the AR(2) process  $X_t = X_{t-1} - 0.25X_{t-2} + e_t$

- i) Obtain the difference equation for autocorrelation function ACF ( $\rho_k$ ) (4 Marks)
- ii) Calculate the values for autocorrelation function  $\rho_k$ , for  $k = 1, 2, 3, \dots, 10$  (5 Marks)
- iii) Compute the partial autocorrelation for lags 1,2,3. (5 Marks)
- iv) What do you expect to be the partial autocorrelation function for lags greater than three? (2 Marks)
- v)
- vi) What does the values of ACF and PACF signify about the order the model? (4 Marks)

**QUESTION FOUR (20 MARKS)**

a) Describe the steps in time series model identification process. (12 Marks)

b) Determine whether the following series is stationary or invertible.

$$x_t = 0.8x_{t-1} + 0.48x_{t-2} + 0.3e_{t-1} - 0.18e_{t-2} + e_t \quad \text{(8 Marks)}$$

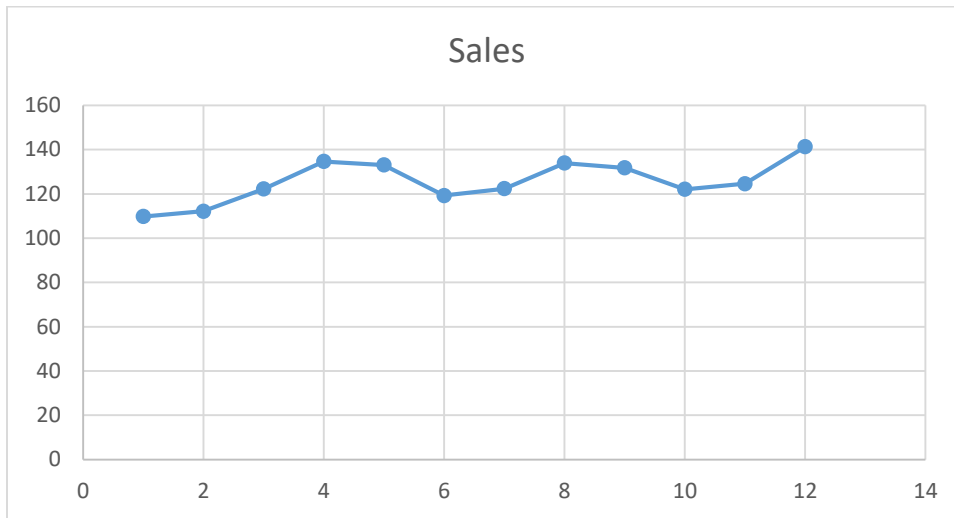
**QUESTION 5 (20 MARKS)**

a) Explain the **three** main stages in time series analysis (4 Marks)

b) Consider the following data whose time series plot is given in Figure 5 below

t	1	2	3	4	5	6	7	8	9	10	11	12
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$X_t$  110 112 122 135 133 119 122 134 132 122 125 141



**Figure 5**

- i) Perform an appropriate transformation to make the data stationary. Let the new series be  $W_t$  **(4 Marks)**
- ii) Plot  $W_t$  and state whether it is stationary or not **(2 Marks)**
- iii) Compute the autocorrelation function (ACF) and partial autocorrelation function (PACF) of  $W_t$  **(8 Marks)**
- iv) Determine the ACF which are significant, using an appropriate confidence interval. **(2 Marks)**